## Math 4050

## Practice Problem Set #7

Problem 7.1 Solve the trigonometric equation over all real numbers:

$$2\cos^2(2x) - 11\cos(2x) + 5 = 0$$

**Problem 7.2** Solve the trigonometric equation over all real numbers. Express your answer in a form that you would plug into a calculator.

$$\sin 3x = \frac{1}{3}$$

Problem 7.3 Simplify

$$\frac{16(\cos 170^{\circ} + i\sin 170^{\circ})}{2(\cos 50^{\circ} + i\sin 50^{\circ})}$$

Express your answer in rectangular form.

Problem 7.4 Solve the equation

$$\tan 2x = -\sqrt{3}$$

**Problem 7.5** Express -5+12i in trigonometric form. Use degree measure (not radians) and express your answer accurate to one decimal place.

Problem 7.6 Find all solutions of

$$\sin x - \sqrt{3}\cos x = -1.$$

*Hint*: Begin by converting the left-hand side into a single trigonometric function.

**Problem 7.7** Use DeMoivre's Theorem to compute  $(-1 + i\sqrt{3})^{102}$ .

Problem 7.8 Exactly compute

 $[3(\cos 41^{\circ} + i \sin 41^{\circ})] [2(\cos 109^{\circ} + i \sin 109^{\circ})]$ 

Express your answer in rectangular form.

**Problem 7.9** Find all solutions to the equation  $z^4 = 3 + 3i$ . Express your answers accurate to three decimal places.

**Problem 7.10** Solve for x on the interval  $[0, 2\pi]$ :

$$\sin 2x + \sin 4x = 0$$

*Hint:* Use a trig identity to get started.