

1. Compute the limit. $\lim_{x \rightarrow 3} (x^2 + 3x - 1)$
 2. Compute the limit. $\lim_{x \rightarrow 1} ((x - 1) \cos x)$
 3. Compute $\lim_{x \rightarrow 2} \frac{3x^3 + 2x^2 + 3x - 38}{x^2 - 3x + 2}$.
 4. Compute $\lim_{t \rightarrow -1} \frac{t^3 + 2t^2 - 4t - 5}{t^3 + t^2 + t + 1}$.
 5. Explain why $\lim_{x \rightarrow -1} \frac{x + 1}{|x + 1|}$ does not exist.
 6. Explain why $\lim_{x \rightarrow 0} \sin \frac{1}{x}$ does not exist.
 7. Explain why $\lim_{x \rightarrow 1} \frac{x^2 + 3x + 1}{x^2 - 3x + 2}$ does not exist.
 8. Use the definition of derivative to compute $f'(x)$ given that $f(x) = 3x^2 + 2x - 9$
 9. Use the definition of derivative to compute $f'(x)$ given that $f(x) = \sqrt{x + 2} + 3$
 10. Use the definition of derivative to compute $f'(x)$ given that $f(x) = \frac{1}{\sqrt[3]{x + 1}}$
 11. Let

$$f(x) = \begin{cases} \frac{\sin 3x}{x} & : x < 0 \\ \frac{\tan 2x}{x} & : 0 < x \\ 0 & : x = 0 \end{cases}$$

Is f continuous at $x = 0$? If so show why. If not, determine if 0 is a removable discontinuity.
 12. Let

$$f(x) = \begin{cases} 2x + c & : x < 1 \\ 5x - c & : 1 \leq x \end{cases}$$
 13. Compute $\lim_{x \rightarrow 0} \frac{\tan x}{x}$.
 14. Compute $\lim_{\theta \rightarrow 0} \frac{1 - \cos^2 \theta}{\theta^2}$.
 15. Compute $\lim_{t \rightarrow 0} \frac{\sin(2t)}{3t}$.
 16. Compute $\lim_{x \rightarrow 3^+} f(x)$ and $\lim_{x \rightarrow 3^-} f(x)$. Does $\lim_{x \rightarrow 3} f(x)$ exist? If so state how you know, if not state why.

$$f(x) = \begin{cases} \sin x & : x \leq 0 \\ x & : 0 < x \leq 3 \\ x^2 - 4 & : x > 3 \end{cases}$$
 17. The function $f(x)$ is given by $f(x) = \frac{x + \sin x}{x}$. Note that $f(0)$ is not defined. Is it possible to assign a value to $f(0)$ to make $f(x)$ continuous at 0? If so, what should $f(0)$ be?
 18. Is there a number c that makes the function f continuous, where f is defined below? If so, find c .

$$f(x) = \begin{cases} x^2 + 3 & : x \leq 1 \\ -2x^2 + c & : x > 1 \end{cases}$$
 19. Compute $\frac{d}{dx}(x^2 \sin(2x))$
 20. Compute $\frac{d}{dx} \frac{x^2 + 1}{x^2 + x - 4}$
- Is there a value of c that makes f continuous at $x = 1$? If so, find c . If not, show why.

21. Compute $\frac{d}{dx}(\tan(x^2 + 3))^3$
22. Compute $\frac{d}{dx}\sqrt[5]{(x^3 + 2)^2}$
23. Compute $\frac{d}{dx}\frac{\sin(2x - 1)}{1 + \sec x}$
24. Compute $\frac{d}{dx}\frac{\csc^2(x^2) + 3}{\pi}$
25. Find an equation of the tangent line to $y = \sin^3 x \cos x$ at the point where $x = \frac{\pi}{4}$.
26. Find an equation of the tangent line to $y = x \sin x$ at the point where $x = \frac{\pi}{3}$.
27. Find an equation of the tangent line to $y = \sqrt{3x - 2}$ at the point where $x = 6$.
28. Find equations for all the lines that pass through the point $(2, 10)$ and are tangent to the graph of $y = x^2 + 2x + 3$. (Note that the point is not on the graph.)
29. Find equations for all the lines that pass through the point $(1, 50/9)$ and are tangent to the graph of $y = \frac{10}{x}$. (Note that the point is not on the graph.)
30. Use the linearization of the appropriate function to estimate $\sqrt[3]{999}$.
31. Explain why radians are easier to use than degrees when doing a calculus problem.
32. Look at the first few derivatives of the function $f(x) = \frac{1}{x}$ and guess a formula for $f^{[n]}(x)$, the n^{th} derivative of $f(x)$.
33. Suppose that $f(x)$ is a polynomial of degree n with leading coefficient 7. (That is, the term with the highest power of x is $7x^n$.) Find a formula for the n^{th} derivative of $f(x)$.
34. Compute y' given that $x^4 + y^4 = a^4$ where a is a constant. Find equations of the lines tangent to this graph at the points where $x = \frac{a}{\sqrt[4]{2}}$.
35. Compute $\frac{dy}{dx}$ given that $x^2y + y^2x - xy = 1$. Also find an equation of the tangent line through $(1, 1)$.
36. The position of an object along a line is given by $x(t) = 10t + \sin(3t)$ where t is measured in seconds and x is measured in meters. Find the object's velocity and acceleration at time t . State the units.
37. The velocity of an object is given by $v(t) = t^2 + 3t - 7$ where the distance units are feet and the time units are seconds. Find a formula for position and a formula for the acceleration and state the units for each.
38. The acceleration of an object is given by $a(t) = 28t$ where the distance unit is meters and the time unit is minutes. Find formulas for the velocity and position of the object. State the units of each.