

1. Let  $f(x) = x^2 + 6x + 13$ .
  - a) First think of the function  $f$  as  $f : \mathbf{R} \rightarrow \mathbf{R}$ . Sketch a graph of  $f$ .
  - b) Now think of  $f : \mathbf{C} \rightarrow \mathbf{C}$ . Find all the complex numbers  $z$  so that  $f(z)$  is a real number.
  - c) Sketch a graph of  $f$  as a function whose domain is the set of all complex numbers  $z$  with  $f(z)$  a real number and range a subset of the reals. The graph will be a three dimensional graph with the domain a subset of the plane and the range a line, as in the class discussion.
  - d) Describe the graph.
2. Let  $f(x) = x^2 - 2x + 10$ . Do parts a), b), c) and d) as in problem 1).
3. Is the following a true statement? Justify your answer.

Let  $f : X \rightarrow Y$  be a function and suppose that  $x_0 \in X$  and  $y_0 \in Y$  satisfy  $(x_0, y_0) \in f$ . If  $(x, y) \in f$  and  $x \neq x_0$ , then  $y \neq y_0$ .
4. Review the interpretations of the first and second derivative of a function. Describe the geometry of the first derivative and the geometry of the second derivative as they relate to the graph of a function. Also, give the interpretation of the first and second derivative if the function is the position of an object at time  $t$  where  $t$  is the variable. Carefully write this up as if you were explaining these interpretations to someone. You may draw pictures to help with your explanations.