

Differential Equations Homework - Find the general solutions and if initial conditions are given, find the specific solution.

1. $y' = 3xy^2$

2. $xy' = \frac{y}{2}$

3. Consider the equation $\frac{dP}{dt} = rP \left(1 - \frac{P}{K}\right)$ where $r > 0$ and $K > 0$ are constants.

a. Find the general solution and simplify your answer.

b. Find $\lim_{t \rightarrow \infty} P(t)$

c. Find all points of inflection for your solution $P(t)$.

4. $y' = \frac{y+1}{x} \quad y(0) = 5$

5. $y' + \frac{2}{x}y = 1 \quad y(3) = 2$

6. $y' - y \tan x = \cos x$

7. $y' + y = x^2$

8. $y' + \frac{x}{2}y = \sin x$

9. $(1+x)y' + y = 0 \quad y(0) = 2$